

# The $p$ - $T$ coexistence line of nuclear matter: ISiS results

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In Fisher's droplet model [1] a non-ideal fluid is approximated by an ideal gas of droplets. Thus, summing over  $n_A$ , the normalized yield of droplets of size  $A$ , gives the total pressure and the reduced pressure is:

$$\frac{p}{p_c} = \frac{T \sum n_A(\Delta\mu, E_{Coul}, T)}{T_c \sum n_A(\Delta\mu, E_{Coul}, T_c)}. \quad (1)$$

The coexistence line for finite neutral nuclear matter is obtained by substituting the  $n_A(\Delta\mu = 0, E_{Coul} = 0, T)$  in the numerator of Eq. (1) and  $n_A(\Delta\mu = 0, E_{Coul} = 0, T_c)$  in the denominator.

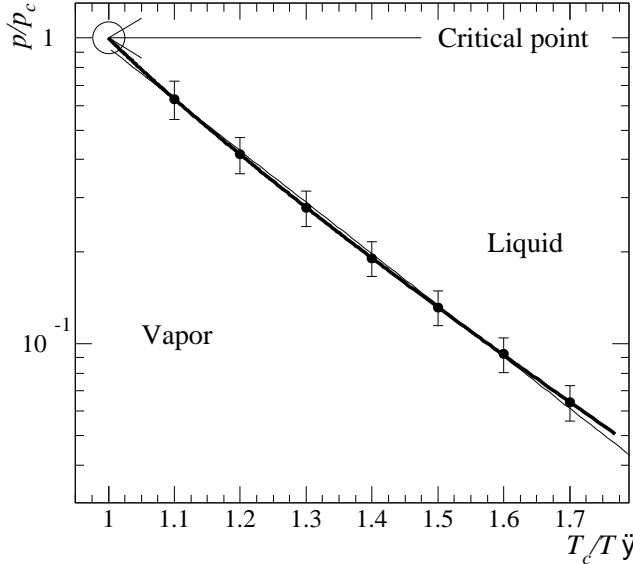


Figure 1: The reduced pressure-temperature phase diagram: the thick line shows the calculated coexistence line, the points show selected calculated errors and the thin line shows a fit to the Clausius-Clapeyron equation.

Figure 1 gives an estimate of the coexistence line of finite neutral nuclear matter, based on an analysis of the ISiS fragment yields of 8 GeV/c  $\pi + \text{Au}$  [1]. From this it is possible to make an estimate of the bulk binding energy of nuclear matter. Beginning with the Clausius-Clapeyron

equation

$$\frac{\partial p}{\partial T} = \frac{\Delta H}{T \Delta V} \quad (2)$$

and solving for the vapor pressure with

$$\Delta V = V_{vapor} - V_{liquid} \approx V_{vapor} = \frac{T}{p} \quad (3)$$

one obtains

$$p = p_0 \exp\left(\frac{-\Delta H}{T}\right) \quad (4)$$

which leads to the ratio of

$$\frac{p}{p_c} = \exp\left[\frac{\Delta H}{T_c} \left(1 - \frac{T_c}{T}\right)\right]. \quad (5)$$

where  $\Delta H$  is the molar enthalpy of evaporation. Equation (5) is empirically observed to describe several fluids up to  $T_c$ .

A fit of Eq. (5) to the coexistence line gives the ratio of  $\Delta H/T_c$ . Using the value of  $T_c = 6.7 \pm 0.2$  MeV [1] gives the molar enthalpy of evaporation of the liquid  $\Delta H = 26 \pm 1$  MeV. From  $\Delta H$   $\Delta E$  is found via  $\Delta E = \Delta H - pV$  with  $pV = T$  using the average temperature from the range in Fig. 1,  $\langle T \rangle \approx 4$  MeV.  $\Delta E$  refers to the cost in energy to evaporate a single *fragment*. To determine the energy cost on a per nucleon basis  $\Delta E$  is divided by the average size of a fragment over the temperature range in Fig. 1. Since the gas described by Fisher's model is an ideal gas of droplets, the average droplet size is greater in size than a monomer and in the region of the  $p$ - $T$  coexistence line is  $\sim 1.5$ . Thus the  $\Delta E/A$  becomes  $\sim 15$  AMeV, close to the nuclear bulk energy coefficient of 15.5 MeV.

## References

- [1] J. B. Elliott *et al.*, Phys. Rev. Lett. **88**, 042701 (2002).